On Specificity in Default Logic

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Abstract

The applicability of lexicographic comparison in nonmonotonic reasoning with specificity is investigated. A priority mechanism based on lexicographic comparison is defined for Rciter's default logic. The following principle - earlier used by Geffner and Pearl in conditional entailment - is used as the basis for specificity-based priorities for normal default theories for each rule there is a context where it ma> not be defeated by any other rule. A method for computing priorities according to the principle is given. Connection to earlier work is discussed.

1 Introduction

Two kinds of weaknesses have been identified m nonmonotonic logics insensitivity to specificity [Poole, 1985] and sensitivity to irrelevant premises |Geffner and Pearl, 1992] Only the first kind of weakness is present in systems that are defined using some form of maxi mal consistency [Reiter, 1980, Moore, 1985, Poole, 1988] In the well-known example, Tweety is a penguin, penguins are birds, penguins usually cannot fly, birds usually can Reiter's default logic does not say anything about the flying ability of Tweety The rule concerning the flying ability of penguins is more specific than the rule about birds, and the rule about penguins should be used Reiter and Cnscuolo [1981] suggest that the application of less specific defaults can be exphcitly blocked by using semi-normal defaults Others introduce priorities [Lifschitz, 1985, Konohge, 1988, Brewka, 1989, Baader and Hollunder, 1993, Brewka, 1994, Rintanen, 1994] Priorities are given as ordenings of predicates, formulae, or default rules in conflicting situations pref erence is given to items with a higher priority

The second land of weakness shows up in logics based on probability [Adams, 1975, Pearl, 1988] and in logics that are defined directly by stating the properties a consequence relation should satiBfy, for example the preferential logics of Kraus et al [1990] These logics give the correct answers in the standard examples about specificity, for instance concerning Tweety's flying ability Their weakness is apparent when a set of premises is extended with an irrelevant premise most of the useful consequences are cancelled For example, if Tweety

is a black penguin, Tweety's inability to fly cannot be inferred

In this paper, we investigate the applicability of lexi cographic priorities as a mechanism for resolving default conflicts according to specificity Our approach is conservative we do not uropose any original notion of specificity To date, the most successful area in defeasible reasoning - from the point of view of handling both specificity and irrelevant premises - is inheritance reasoning [Hortj, 1994] Therefore it seems desirable that solutions to these problems in a more general setting would subsume some form of inheritance reasoning Different inheritance theories propose different specificity notions A weak but reasonable principle that is found for example in the preferential logics of Kraua et al and that is also respected by inheritance theories is the following given a default that allows the conclusion of 0 from a, the premise a and no other premises, conclude /? This principle is used in the definition of conditional entailment [Geffner and Pearl, 1992] and we shall use it in deriving priorities from specificity We strengthen Reitcr's default logic with a priority mechanism that uses lexicographic comparison Lexicographic comparison has been used in earlier work on explicit priorities, for example in [Lifschitz, 1985, Brewka, 1989 Geffner and Pearl, 1992, Ryan, 19921

The outline of the paper is as follows. In Section 2 we present the specificity notion, and in Section 3 we extend default logic with a priority mechanism. In Section 4 we show how nonmonotonic reasoning that respects the specificity notion can be achieved in the extended default logic and how it subsumes an inheritance theory. In Section 5 we discuss how the specificity principle is too weak for default theories in general, claim that priority mechanisms that lexicographically order extensions or models are in general too weak for achieving inheritance-like reasoning, and discuss the possibility of stronger priorities in more general but still restricted cases

2 Specificity in default logic

Many formalizations of defeasible reasoning that address specificity [Kraue et al, 1990, Lehmann and Magidor, 1992, Adams, 1975, Pearl, 1988, 1990, Goldszmidt et al, 1990] employ or fulfill a principle not fulfilled by default logic For default theories (D,BUC) with normal de-

faults D the principle can be expressed as follows

$$(D, B \cup \{\alpha\}) \models_x \beta \text{ for all defaults } \frac{\alpha - \beta}{\beta} \in D$$
 (1)

Above D is the set of default rules of a default theory, B is a set of sentences that forms the background¹, and \models_x is a consequence relation. The consequence relation usually discussed in the context of default logic is cautious reasoning $\Delta \models_c \phi$, which means that the formula ϕ is contained in all extensions of the default theory Δ . This consequence relation does not fulfill Condition 1

Example 2 1 Consider the following set of defaults D

$$\frac{P \quad B}{B} \quad \frac{B \quad F}{F} \quad \frac{P \quad \neg F}{\neg F}$$

The default theory $\Delta = \langle D, \{P\} \rangle$ has two extensions Both contain P and B, one contains $\neg F$ and the other contains F. Therefore $\Delta \not\models_{\epsilon} \neg F$.

In ϵ -semantics [Pearl, 1988] a counterpart of Condition 1 is directly justified by the definition of conditional probability. Outside probabilistic systems, this condition has been used for example by Poole [1991]. A default can be viewed as expressing a rule that applies unconditionally in the context specified by the antecedent of the rule. In Example 2.1 above, if P is read as "x is a penguin", B as "x is a bird", and F as "x is able to fly". If B is all the information available, conclude that x flies. If P is all the information available, conclude that x does not fly

Consequence relations for default logic that treat specificity properly should fulfill at least Condition 1. As shown above, \models_{c} is not such a relation. A natural way to strengthen it is to consider only a subset of the extensions, those in which conflicts are resolved without violating specificity, and take their intersection. Such a subset can be selected for example by lexicographic comparison

3 Priorities in default logic

Lexicographic priorities in the context of expressive non-monotonic logics have been earlier investigated in [Rintanen, 1994]. In that paper a definition of preferred stable expansions for autoepistemic logic was given. A similar definition can be devised for default logic. The significance of defaults is represented by a strict partial order, that is, a transitive and asymmetric relation $\mathcal P$. If defaults δ and δ' are related as $\delta \mathcal P \delta'$, then the application of δ is more desirable than the application of δ' . The default δ has higher priority

Below, \mathcal{L} denotes the language of the propositional logic, and \mathcal{D} the set of all defaults $\frac{\alpha \beta}{\beta}$ where $\{\alpha, \beta\} \subseteq \mathcal{L}$

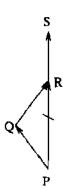


Figure 1 An extended penguin triangle

Definition 3 1 (Application) A default $\frac{\alpha \beta}{\beta}$ is applied in $E \subseteq \mathcal{L}$, if $\alpha \wedge \beta \in E$ This is written as $app(\frac{\alpha \beta}{A}, E)$

Definition 3 2 (Preferred extensions) Let $\Delta = (D,W)$ be a default theory, and $\mathcal P$ a strict partial order on D. Let E be an extension of Δ . Then E is a $\mathcal P$ -preferred extension if there is a strict total order $T \supseteq \mathcal P$ on D such that for all extensions E' of Δ , for all $\delta \in D$,

$$app(\delta, E' \setminus E)$$
 implies that for some $\delta' \in D$, $\delta' T \delta$ and $app(\delta', E \setminus E')$

Definition 3.3 The fact that formula ϕ is contained in all \mathcal{P} -preferred extensions of Δ is written as $\Delta \models_{\mathcal{P}} \phi$

Example 3.1 For the default theory (D,\emptyset) depicted in Figure 1 the following priorities are needed

$$\mathcal{P} = \{\langle \frac{P - \neg R}{\neg R} \ \frac{Q - R}{R} \rangle, \langle \frac{P - \neg R}{\neg R}, \frac{R - S}{S} \rangle\}$$

The default theory $\langle D, \{P\} \rangle$ has two extensions that respectively apply $\{\frac{P-R}{-R}, \frac{PQ}{Q}\}$ and $\{\frac{PQ}{Q}, \frac{QR}{R}, \frac{RS}{S}\}$. Only the first one is \mathcal{P} -preferred. The two extensions and all strict total orders $\mathcal{T} \supseteq \mathcal{P}$ on the defaults are depicted below on the left (the default $\frac{PQ}{Q}$ is omitted because it is applied in both extensions). The most significant defaults are the lowest. Application is depicted as • and non-application as •

If $(\frac{P-R}{-R}, \frac{RS}{S})$ were omitted in \mathcal{P} , the strict total order $\frac{RS}{S}, \frac{P-R}{-R}, \frac{PQ}{Q}, \frac{QR}{R}$ would extend \mathcal{P} , and consequently there would be a \mathcal{P} preferred extension in which $\frac{PR}{R}$ were not applied. The diagram on the right depicts the unwanted total order

¹This – possibly controversial – division between back ground B and evidence C (necessary and contingent facts) is made in all the afore-mentioned formalisms that address specificity. The background may affect the priorities, the evidence may not

4 Specificity-based priorities

Pre-computed explicit priorities are useful if the computation can be performed once and the priorities can be used in answering a wide variety queries concerning the knowledge base Priorities for a default theory $\{D, BuC\}$ depend only on the defaults D and the background B As long as changes are made only to the contingent information C, no recomputation of priorities is needed

Next we show how Condition 1 can be fulfilled in default logic with the lexicographic prionty mechanism defined in the preceding section

Definition 4.1 Let (D,B) be a default theory and f a function from $D \times 2^D \times 2^L$ to 2^D Define $\mathcal{P}_{\Delta f}$ as follows

$$D_{0} = \{\frac{\alpha - \beta}{\beta} \in D | \langle D, B \cup \{\alpha\} \models_{c} \beta \}$$

$$D_{i+1} = \{\delta \in D \setminus \bigcup_{0 \le k \le i} D_{k} | f(\delta | D, B) \subseteq \bigcup_{0 \le k \le i} D_{k} \}$$

$$P_{0} = \emptyset$$

$$P_{i+1} = \{\langle \delta, \delta' \rangle | \delta \in D_{i+1}, \delta' \in f(\delta, D, B) \}$$

$$P_{\Delta | f} = \text{the transitive closure of } \bigcup_{i \ge 0} P_{i}$$

If $D_0 \cup \dots \cup D_n = D$ for no $n \ge 0$, then we leave $\mathcal{P}_{\Delta f}$ undefined

Given a function f, the above definition imposes an ordering on defaults. For a default δ , $f(\delta,D,B)$ can be thought of as the set of defaults that may become applied if a default conflict is resolved so that Condition 1 or some stronger specificity notion is violated. To avoid this, δ has to be given a higher priority than any of the defaults in $f(\delta,D,B)$. Violation of Condition 1 is sometimes unavoidable, for example when $D = \{\frac{AB}{B}, \frac{A-B}{B}\}$

Next we give one such function f The notation $\Delta \models_b \phi$ means that ϕ is in at least one extension of Δ

Theorem 4.2 Let $\Delta = (D, B)$ Define $f_1(\frac{\alpha \beta}{6}, D, B)$ as

$$\begin{cases} \delta \in D | \ E \ \text{ and } E' \ \text{ are extensions of } \langle D, B \cup \{\alpha\} \rangle, \\ app(\delta, E' \backslash E), app(\frac{\alpha}{\beta}, E \backslash E'), \\ \text{ for no extension } E'' \ \text{ of } \langle D, B \cup \{\alpha, \beta\} \rangle \\ \{\delta \in D | app(\delta, E' \backslash E'') \ \text{ or } app(\delta, E'' \backslash E') \} \subset \\ \{\delta \in D | app(\delta, E \backslash E') \ \text{ or } app(\delta, E' \backslash E) \} \}$$

Then $\models_{\mathcal{P}_{\Delta} J_1}$ fulfills Condition 1 for $\langle D, B \rangle$

Proof The relation $\mathcal{P}=\mathcal{P}_{\Delta|f_1}$ is transitive and asymmetric by construction. Let $\frac{\alpha\beta}{\beta}$ be any default in D_0 . Clearly $\langle D,B\cup\{\alpha\}\rangle\models_{\mathcal{P}}\beta$. Let $\delta=\frac{\alpha\beta}{\beta}$ be any default in D_i for some $i\in\{1,\dots,n\}$. Let $T\supseteq\mathcal{P}$ be any strict total order on D. Let E' be any extension of Δ that does not apply $\frac{\alpha\beta}{\beta}$ (hence $\neg\beta\in E'$). By construction, there is an extension E of $\langle D,B\cup\{\alpha,\beta\}\rangle$ such that for all defaults δ' such that $\operatorname{app}(\delta',E'\backslash E)$, $\delta\mathcal{P}\delta'$. Hence $\delta\mathcal{T}\delta'$, and E' cannot be \mathcal{P} -preferred. Therefore all \mathcal{P} preferred extensions contain β .

Gelfond and Przymusinska [1990] present theories of inheritance that are based on translating inheritance networks into sets of formulae in autoepistemic logic. In Section 4b of their paper, they give two formalizations of inheritance. It turns out that the one that explicitly orders extensions of an inheritance network is closely related to our definition of specificity-based priorities and our priority mechanism². Our result below provides a conceptual simplification of Gelfond's and Przymusinska's work reification of inheritance networks is avoided as links can be directly represented as default rules, and the ordering on extensions is justified by Condition 1. We restrict to inheritance networks with only defeasible links between classes. Strict links require stronger priorities or non-normal defaults.

Theorem 4.3 Assume that G is an inheritance network with only one object x, and that there are no strict links between classes. The translation of G into default logic is $\Delta = \langle D, B \cup C \rangle$, where

$$D = \left\{ \frac{P - Q}{Q} \middle| \text{ there is link } P \to Q \text{ in } G \right\}$$

$$\cup \left\{ \frac{P - Q}{\neg Q} \middle| \text{ there is link } P \neq Q \text{ in } G \right\}$$

$$B = \emptyset$$

$$C = \left\{ P \middle| \text{ there is a strict link } x \Rightarrow P \text{ in } G \right\}$$

$$\cup \left\{ \neg P \middle| \text{ there is a strict link } x \not\Rightarrow P \text{ in } G \right\}$$

Let $P\Delta$ f1 be the priorities for A as given in Definition 4.1 Then for any proposittional variable P, P belongs to all $P\Delta$ f1 preferred extensions of Δ if and only H(x,P) belongs to all belief sets of Th(G)

Condition 1 imposes only a lower bound on the consequence relation Reasoning with lexicographic priorities is monotonic with respect to the priorities the more priorities there are, the more conclusions can be obtained Consider the Nixon Diamond No priorities on the defaults involved violate Condition 1 Some priorities prefer "quakers are pacifists" to "republicans are not pacifists" There is no reason for this It would seem that demanding that priorities are minimal would solve this problem This is not the case

$$\{\frac{P - Q}{Q} - \frac{P - A \vee B}{A \vee B} - \frac{Q - A}{\neg A} - \frac{Q - B}{\neg B}\}$$

If the second default is preferred to one or both of the last two, Condition 1 is satisfied However, minimal such priorities give arbitrarily preference to one of the last two defaults. In conditional entailment jGeffner and Pearl, 1992], this problem is avoided by considering all (minimal) priorities. There is no obvious way to formalize this requirement about the fairness of priorities. Our priorities are not minimal and do not seem to be unfair because defaults are treated symmetrically in cases like the above

² On page 412 in J Gelfond and Przymusinska, 1990], the relation *better* is defined. The results in the paper assume that this relation is asymmetric although it is not. Our results use a corrected definition.

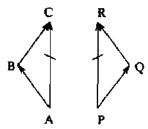


Figure 2 Two independent penguin triangles

5 Beyond inheritance networks

Example 3 1 demonstrates that it is not sufficient to prioritize defaults the conclusions of which arc contradictory. To guarantee that a conflict is solved properly, it is necessary to give a lower priority also to those defaults that potentially become applied if a conflict is resolved in a wrong way. In inheritance networks, these defaults can be easily identified, as shown in Section 4. This is not the case with default theories in general. Next we give a variant of Example 3.1

Example 5 1 Let $\Delta = \langle D, \emptyset \rangle$ where

$$D = \{\frac{P - \gamma R}{-\overline{R}}, \frac{P - Q}{Q}, \frac{Q - R}{R}, \frac{R \wedge 4 - S}{S}\}$$

Priorities according to Definition 4.1 are $\mathcal{P}_{\Delta f_1} = \{(\frac{P \neg R}{\neg R}, \frac{Q R}{R})\}$, but $(D, \{P A\}) \not\models_{P_{\Delta f_1}} \neg R$ The conclusions with $\mathcal{P}_{\Delta f_1}$ are too weak

This is a problem not recognized in earlier work on lex icographic priority mechanisms. To overcome it it does not suffice to consider Condition 1 only A more general definition of specificity has to be devised. Such A definition should cover also cases where the contingent sentences are not just a prerequisite of one default. As hinted in Example 5.1, the contingent facts may in an intricate way affect the set of defaults that potentially become applied. As priorities are to be independent of the contingent facts, this creates new challenges for the definition of specificity based priorities, as illustrated in the following example.

Example 5 2 Consider the defaults D in Figure 2 We want $\langle D, \{A, C \to P\} \rangle \models_{\mathcal{P}} \neg C$ We also want $\langle D, \{P, R \to A\} \rangle \models_{\mathcal{P}} \neg R$ To fulfill these requirements respectively the priorities $\frac{A \neg C}{\neg C} \mathcal{P} \frac{P \neg R}{\neg R}$ and $\frac{P \neg R}{\neg R} \mathcal{P} \frac{A \neg C}{\neg C}$ are needed. Hence no \mathcal{P} fulfills these requirements.

Similar examples can be constructed for other systems of prioritized nonmonotonic reasoning that order exten sions or classical models by lexicographic or other form of comparison, for example [Geffner and Pearl, 1992, Brewka, 1989, Lifechitz, 1985, Ryan, 1992, Gardenfors and Makinsoji, 1994] The presence of disjunctive for mulae in the sets of contingent facts is an obstacle to the possibility of inhentance-like reasoning in systems of default reasoning that use fixed priorities with lexicographic comparison

A natural line of research is to consider cases where the contingent facts may not contain the kind of problematic implicational formulae used in Example 5.2. A suitable restriction is to require that the consistent facts are propositions! variables or their negations. With this restriction satisfactory defeasible reasoning with specificity can hopefully be achieved for a wide class of default theories.

6 Alternative definitions of prioritized reasoning

The priority mechanism introduced in Definition 3 2 is on!) one of several alternatives That definition classifies defaults to those that are applied in an extension and to those that are not Another reasonable classification is to defaults that are not defeated and to defaults that are defeated

Definition 6 1 (Defeat) A default $\frac{\alpha \beta}{\beta}$ is defeated in $E \subseteq \mathcal{L}$, if $\alpha \land \neg \beta \in E$

For prerequisite-free defaults application and non-defeat coincide. The notions differ for a default $\frac{\alpha \beta}{\beta}$ and an extension E when the prerequisite α is not in E. Then $\frac{\alpha \beta}{\beta}$ is neither defeated nor applied in E. Another choice – orthogonal to the choice between application and non-defeat – is the way partiality in the priority partial orders is interpreted

Definition 6 2 (Preferred2 extensions) Let $\Delta = \langle D, W \rangle$ be a default theory, and $\mathcal P$ a strict partial order on D. Let E be an extension of Δ . Then E is a $\mathcal P$ preferred2 extension if for all extensions E' of Δ , there is a strict total order $T \supseteq \mathcal P$ on D such that for all $\delta \in D$,

$$app(\delta E' \setminus E)$$
 unplies that for some $\delta' \in D$,
 $\delta' T \delta$ and $app(\delta', E \setminus E')$

Each "P-preferred extension is P-preferred2 but not vice versa. The generalization of lexicographic comparison to partially ordered positions as given in the definition of preferred hat, been earlier used by Brewka [1989]. The generalization used in preferred2 has been earlier used for example by Gfffner and Pearl [1992] and Ryan [1992]. The last two do not explicitly reduce lexicographic comparison with partially ordered positions to lexicographic comparison with totally ordered positions. Brewka performs lexicographic comparison implicitly in a procedure for computing preferred sets of formulae

There are no obvious differences in the expressivity of the priority mechanisms suggested by the above definitions and the one given in Section 3. A theorem corresponding to Theorem 4.3 for a priority mechanism that uses defeat instead of application requires stronger priorities than those obtained merely on the basis of Condition 1. The reason for this is that in inheritance networks, the number of defaults that are potentially defeated in the intended extensions but not in the unintended extensions, may be increased by extending the set of contingent facts with propositional atoms

7 Related work

Pearl's system Z is an improvement over p-entailment [Adams, 1975) and preferential logics of Kraus, Lehmann and Magidor [1990] because it handles irrelevant premises satisfactorily System Z imposes an ordering on defaults (the Z-ordenng), and models of the defaults are ordered according to the highest defeated default. This introduces a new kind of weakness if a member of some class is in some respect exceptional, it is allowed to be exceptional in other respects as well Conditional entailment of Geffner and Pearl [1992] remedies this problem comparison by highest defeated default is replaced by lexicographic comparison that considers significant also violations to defaults below the highest defeated one Instead of the Z-ordenng, all strict partial orders that together with lexicographic comparison - satisfy a counterpart of Condition 1, are used Within our framework, conditional entailment can be defined as follows

Definition 7.1 Let D_c be a set of defaults $\alpha \Rightarrow \beta$ and $B \subseteq \mathcal{L}$ a set of formulae Let $D = \{\frac{\top \alpha \rightarrow \beta}{\alpha \rightarrow \beta} | \alpha \Rightarrow \beta \in D_c\}$ Then $\langle (D_c, B), C \rangle$ conditionally entails γ , if γ is in all \mathcal{P} -preferred₂ extensions of $(D, B \cup C)$ for all \mathcal{P} such that $(D, B \cup \{\alpha\}) \models_{\mathcal{P}} \beta$ for all $\alpha \Rightarrow \beta \in D_c$

Delgrande and Schaub [1994] and Brewka [1994] present methods for computing priorities for Reiter's default logic Both identify minimal sets of conflicting defaults, Delgrande and Schaub directly using the Z-ordenng of Pearl, and Brewka using a closeh related idea that takes into account the fact that default rules are unidirectional Delgrande and Schaub do not use priorities explicitly, but translate sets of defaults and the priority information to sets of semi-normal defaults rules Brewka [1994] uses the priorities within his prioritized default logic that is based on a variant of Reiter's semiconstructive definition of extension Similar priority mechanisms have been independently investigated elsewhere [Marek and Truszczynski, 1993, Baader and Hollunder, 1993] Neither Delgrande and Schaub nor Brewka verify their systems against any correctness criteria or otherwise explicate the specificity notion they use Both systems seem to fulfill Condition 1

Default logic with specificity as defined in this paper differs in some aspects from most of the inheritance theories. The priorities are fixed, that is, they are the same for all extensions and all sets C of contingent information. Theories of inheritance have priorities implicitly hidden in the definition of preemption. There are examples where fixed priorities necessarily seem to produce too strong conclusions [Horty, 1994]

8 Conclusions

We have extended Reiter's default logic with a lexicographic priority mechanism and presented a method for computing priorities according to specificity. The method produces priorities that are sufficiently strong for inheritance networks. Relaxing two restrictions made in inheritance networks - only propositional atoms as prerequisites and factual knowledge that is not disjunctive - reveals the priorities insufficient. It seems that

non-atomic prerequisites can be handled with a lexicographic priority mechanism for a large class default theories, but disjunctive contingent facts cannot

Our research is closely related to Geffher's and Pearl's work on conditional entailment [Geffner and Pearl, 1992] Conditional entailment does not support inheritance reasoning Delgrande [1994] extends conditional entailment towards inheritance reasoning Our results are likely to have implications on research on that topic

The computation of priorities from specificity is rather complex and tightly intertwined with default reasoning itself. In argument-based systems of defeasible reasoning [Simari and Loui, 1992, Pollock, 1994] these two things are combined there is no division between the reasoning and priority components in these systems. This raises questions concerning the usefulness of such division, for example from the computational point of view.

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