NSGA-Net: Neural Architecture Search using Multi-Objective Genetic Algorithm (Extended Abstract)*

Zhichao Lu, Ian Whalen, Yashesh Dhebar, Kalyanmoy Deb, Erik Goodman, Wolfgang Banzhaf and Vishnu Naresh Boddeti

Michigan State University

{luzhicha,whalenia,dhebarya,kdeb,goodman,banzhafw,vishnu}@msu.edu

Abstract

Convolutional neural networks (CNNs) are the backbones of deep learning paradigms for numerous vision tasks. Early advancements in CNN architectures are primarily driven by human expertise and elaborate design. Recently, neural architecture search (NAS) was proposed with the aim of automating the network design process and generating task-dependent architectures. This paper introduces NSGA-Net – an evolutionary search algorithm that explores a space of potential neural network architectures in three steps, namely, a population initialization step that is based on prior-knowledge from hand-crafted architectures, an exploration step comprising crossover and mutation of architectures, and finally an exploitation step that utilizes the hidden useful knowledge stored in the entire history of evaluated neural architectures in the form of a Bayesian Network. The integration of these components allows an efficient design of architectures that are competitive and in many cases outperform both manually and automatically designed architectures on CIFAR-10 classification task. The flexibility provided from simultaneously obtaining multiple architecture choices for different compute requirements further differentiates our approach from other methods in the literature.

1 Introduction

Deep convolutional neural networks have been overwhelmingly successful in a variety of computer-vision-related tasks like object classification, detection, and segmentation. One of the main driving forces behind this success is the introduction of many CNN architectures, including GoogLeNet [Szegedy et al., 2015], ResNet [He et al., 2016], DenseNet [Huang et al., 2017], etc., in the context of object classification. Concurrently, architecture designs such as ShuffleNet [Zhang et al., 2018], MobileNet [Sandler et al., 2018], LBCNN [Juefei-Xu et al., 2017], etc., have been developed with the goal of

enabling real-world deployment of high-performance models on resource-constrained devices. These developments are the fruits of years of painstaking efforts and human ingenuity.

Neural architecture search (NAS), on the other hand, presents a promising path to alleviate this painful process by posing the design of CNN architectures as an optimization problem. By altering the architectural components in an algorithmic fashion, novel CNNs can be discovered that exhibit improved performance metrics on representative datasets. The huge surge in research and applications of NAS indicate the tremendous academic and industrial interest NAS has attracted, as teams seek to stake out some of this territory. It is now well recognized that designing bespoke neural network architectures for various tasks is one of the most challenging and practically beneficial component of the entire Deep Neural Network (DNN) development process, and is a fundamental step towards automated machine learning.

In this paper, we present NSGA-Net, a multi-objective genetic algorithm for NAS to address the aforementioned limitations of current approaches. A pictorial overview of NSGA-Net is provided in Figure 1. The salient features of NSGA-Net are, (1) multi-objective optimization: Real-world deployment of NAS models demands small-sized networks, in addition the models being accurate. For instance, we seek to maximize performance on compute devices that are often constrained by hardware resources in terms of power consumption, available memory, available FLOPs, and latency constraints, to name a few. NSGA-Net is explicitly designed to optimize such competing objectives. (2) Flexible architecture **search space**: The search space for most existing methods is restricted to a block that is repeated as many times as desired. In contrast, NSGA-Net searches over the entire structure of the network. This scheme overcomes the limitations inherent in repeating the same computation block throughout an entire network, namely, that a single block may not be optimal for every application and it is desirable to allow NAS to discover architectures with different blocks in different parts of the network. (3) Non-dominated sorting: The core component of NSGA-Net is the Non-Dominated Sorting and Crowding distance based multi-objective selection module from NSGA-II [Deb et al., 2002], a multi-objective optimization algorithm that has been successfully employed for solving a variety of multi-objective problems [Tapia and Coello, 2007; Pedersen and Yang, 2006]. Here, we leverage its ability to

^{*}This is an extended abstract of the original paper [Lu *et al.*, 2019], which won the best-paper award at the *GECCO-2019* under Evolutionary Machine Learning track.

Figure 1: Overview of the stages of NSGA-Net. Networks are represented as bit strings, trained through gradient descent, ranking and selection by NSGA-II, search history exploitation through BOA. Output is a set of networks that span a range of complexity and error objectives.

maintain a diverse trade-off frontier between multiple conflicting objectives, thereby resulting in a more effective and efficient exploration of the search space. (4) **Efficient recombination**: In contrast to state-of-the-art evolution-based NAS methods [Real et al., 2017; Real et al., 2019] in which only mutation is used, we employ crossover (in addition to mutation) to combine networks with desirable qualities across multiple objectives from the diverse frontier of solutions, and finally (5) **Bayesian learning**: We construct and employ a Bayesian Network inspired by the Bayesian Optimization Algorithm (BOA) [Pelikan et al., 1999] to fully utilize the promising solutions present in our search history archive and the inherent correlations between the layers of the network architecture.

We demonstrate the efficacy of NSGA-Net on CIFAR10 [Krizhevsky *et al.*, 2009] image classification task by minimizing two objectives: classification error and computational complexity. Here, computational complexity is defined by the number of floating-point operations (FLOPs) that a network carries out during a forward pass. Experimentally, we observe that NSGA-Net can find a set of network architectures containing solutions that are significantly better than hand-crafted methods in both objectives, while being competitive with single objective state-of-the-art NAS approaches. Furthermore, by fully utilizing a population of networks through recombination and utilization of the search history, NSGA-Net explores the search space efficiently and requires less computational time for search than other competing methods.

2 Proposed Approach

Compute devices are often constrained by hardware resources in terms of their power consumption, available memory, available FLOPs, and latency constraints. Hence, real-world design of DNNs are required to balance these multiple objectives (e.g., predictive performance and computational complexity). Often, when multiple design criteria are considered simultaneously, there may not exist a single solution that performs optimally in all desired criteria, especially with competing objectives. Under such circumstances, a set of solutions that provide representative trade-off information between the objectives is more desirable. This enables a practitioner to analyze the importance of each criterion, depending on the application, and to choose an appropriate solution on the trade-off frontier for implementation. We propose NSGA-Net, a genetic algorithm based architecture search method to automatically generate a set of DNN architectures that approximate the Pareto-front between performance and complexity on an image classification task. The rest of this section describes the encoding scheme,

and main components of NSGA-Net in detail.

2.1 Encoding

Genetic algorithms, like any other biologically inspired search methods, often do not directly operate on *phenotypes*. From the biological perspective, we may view the DNN architecture as a phenotype, and the representation it is mapped from as its *genotype*. As in the natural world, genetic operations like crossover and mutation are only carried out in the genotype space; such is the case in NSGA-Net as well. We refer to the interface between the genotype and the phenotype as *encoding* in this paper.

Most existing CNN architectures can be viewed as a composition of computational blocks that define the layer-wise computation (e.g. ResNet blocks [He et~al., 2016], DenseNet block [Huang et~al., 2017], and Inception block [Szegedy et~al., 2015], etc.) and a scheme that specifies the spatial resolution changes. For example, down-sampling is often used after computational blocks to reduce the spatial resolution of information going into the next computational blocks in image classification DNNs. In NSGA-Net, each computational block, referred to as a phase, is encoded using the method presented by [Xie and Yuille, 2017], with the small change of adding a bit to represent a skip connection that forwards the input information directly to the output bypassing the entire block. And we name it as the $Operation~Encoding~\mathbf{x_0}$ in this study.

Operation Encoding $\mathbf{x_o}$. Unlike most of the hand-crafted and NAS generated architectures, we do not repeat the same phase (computational block) to construct a network. Instead, the operations of a network are encoded by $\mathbf{x_o} = \left(\mathbf{x_o^{(1)}}, \mathbf{x_o^{(2)}}, \dots, \mathbf{x_o^{(n_p)}}\right)$ where n_p is the number of phases.

Each $\mathbf{x}_{o}^{(i)}$ encodes a directed acyclic graph consisting of n_{o} number of nodes that describes the operation within a phase using a binary string. Here, a *node* is a basic computational unit, which can be a single operation like convolution, pooling, batch-normalization [Ioffe and Szegedy, 2015] or a sequence of operations. This encoding scheme offers a compact representation of the network architectures in genotype space, yet is flexible enough that many of the computational blocks in hand-crafted networks can be encoded, e.g. VGG [Simonyan and Zisserman, 2015], ResNet [He *et al.*, 2016] and DenseNet [Huang *et al.*, 2017]. Figure 2 and Figure 3 shows examples of the operation encoding.

Search Space. With a pre-determined scheme of spatial resolution reduction (similarly in [Zoph *et al.*, 2018; Real *et al.*,

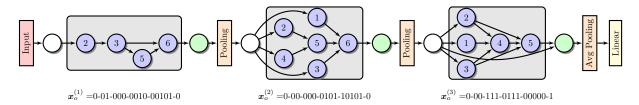


Figure 2: Encoding: Illustration of a classification network encoded by $\mathbf{x} = \mathbf{x}_o$, where \mathbf{x}_o is the operations at a phase (gray boxes, each with a possible maximum of 6 nodes). In this example the spatial resolution changes (orange boxes that connect the phases) are fixed based on prior knowledge of successful approaches. The phases are described by the bit string \mathbf{x}_o which is formatted for readability above. The bits are grouped by dashes to describe what node they control. See Section 2.1 for detailed description of the encoding schemes.

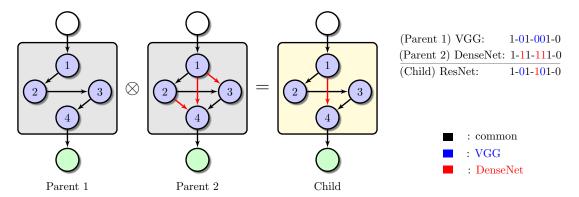


Figure 3: Crossover Example: A crossover (denoted by \otimes) of a VGG-like structure with a DenseNet-like structure may result in a ResNet-like network. In the figure, red and blue denotes connections that are unique to VGG and DenseNet respectively, and black shows the connections that are common to both parents. All black bits are retained in the final child encoding, and only the bits that are not common between the parents can potentially be selected at random from one of the parent.

2019; Liu *et al.*, 2019]), the total search space in the genotype space is governed by our operation encoding x_0 :

$$\Omega_{\mathbf{x}} = \Omega_{\mathbf{x_o}} = n_p \times 2^{n_o(n_o - 1)/2 + 1}$$

where n_p is the number of phases (computational blocks), and n_o is the number of nodes (basic computational units) in each phase. However, for computationally tractability, we constrain the search space such that each node in a phase carries the same sequence of operations, i.e. a 3×3 convolution followed by batch-normalization and ReLU.

It is worth noting that, as a result of nodes in each phase having identical operations, the encoding between genotype and phenotype is a many-to-one mapping. Given the prohibitive computational expense required to train each network architecture before its performance can be assessed, it is essential to avoid evaluating genomes that decode to the same architecture. We develop an algorithm to quickly and approximately identify these duplicate genomes (see [Lu *et al.*, 2019] for details).

2.2 Search Procedure

NSGA-Net is an iterative process in which initial solutions are made gradually better as a group, called a *population*. In every iteration, the same number of offspring (new network architectures) are generated from parents selected from the population. Each population member (including both parents and offspring) compete for both survival and reproduction (becoming a parent) in the next iteration. The initial population may be generated randomly or guided by prior-knowledge (e.g.

seeding the hand-crafted network architectures into the initial population). Following initialization, the overall NSGA-Net search proceeds in two sequential stages, an *exploration* and *exploitation*.

Exploration. The goal of this stage is to discover diverse ways of connecting nodes to form a phase (computational block). Genetic operations, crossover and mutation, offer an effective mean to realize this goal.

Crossover. The implicit parallelism of population-based search approaches can be unlocked when the population members can effectively share (through crossover) building-blocks [Holland, 1975]. In the context of NAS, a phase or the substructure of a phase can be viewed as a building-block. We design a homogeneous crossover operator, which takes two selected population members as parents, to create offspring (new network architectures) by inheriting and recombining the building-blocks from parents. The main idea of this crossover operator is to 1) preserve the common building-blocks shared between both parents by inheriting the common bits from both parents' binary bit-strings; 2) maintain, relatively, the same complexity between the parents and their offspring by restricting the number of "1" bits in the offspring's bit-string to lie between the number of "1" bits in both parents. The proposed crossover allows selected architectures (parents) to effectively exchange phases or sub-structures within a phase. An example of the crossover operator is provided in Figure 3.

Mutation. To enhance the diversity (having different network architectures) of the population and the ability to escape

Architectures	Params (M)	Test Error (%)	MAdds (M)	Search Cost (GPU-days)	Search Method
Wide ResNet [Zagoruyko and Komodakis, 2016]	36.5	4.17	-	-	manual
DenseNet-BC ($k = 40$) [Huang et al., 2017]	25.6	3.47	-	-	manual
NAS [Zoph and Le, 2016]	7.1	4.47	-	3150	RL
NAS + more filters [Zoph and Le, 2016]	37.4	3.65	-	3150	RL
ENAS [Pham et al., 2018]	21.3	4.23	-	0.5	RL + WS
ENAS + more filters [Pham et al., 2018]	38.0	3.87	-	0.5	RL + WS
NSGA-Net	3.3	3.85	1290	8	EA
DARTS second order + cutout [Liu et al., 2019]	3.3	2.76	-	4	WS
NASNet-A + cutout [Zoph et al., 2018]	3.3	2.65	-	2,000	RL
ENAS + cutout [Pham et al., 2018]	4.6	2.89	-	0.5	RL + WS
AmoebaNet-A [Real et al., 2019]	3.2	3.34	-	3,150	EA
NSGA-Net (6 @ 560) + cutout	3.3	2.75	535	4	EA
NSGA-Net (7 @ 1536) + cutout	26.8	2.50	4147	4	EA

Table 1: Comparison of NSGA-Net with baselines on CIFAR-10 image classification. In this table, the first block presents architectures designed by human experts. The second block presents NAS methods that design the entire network. The last block presents NAS methods that design modular blocks which are repeatedly combined to form the final architecture. We use (N @ F) to indicate the configuration of each model, where N is the number of repetition and F is the number of filters right before classification. WS stands for weight sharing.

from local optima, we use a bit-flipping mutation operator, which is commonly used in binary-coded genetic algorithms. Due to the nature of our encoding, a one bit flip in the genotype space could potentially create a completely different architecture in the phenotype space. Hence, we restrict the number of bits that can be flipped to be at most one for each mutation operation. As a result, only one of the phase architectures can be mutated at one time.

Exploitation. The exploitation stage follows the exploration stage in NSGA-Net. The goal of this stage is to exploit and reinforce the patterns commonly shared among the past successful architectures explored in the previous stage. The exploitation step in NSGA-Net is heavily inspired by the Bayesian Optimization Algorithm (BOA) [Pelikan et al., 1999] which is explicitly designed for problems with inherent correlations between the optimization variables. In the context of our NAS encoding, this translates to correlations in the blocks and paths across the different phases. Exploitation uses past information across all networks evaluated to guide the final part of the search. More specifically, say we have a network with three phases, namely $\mathbf{x}_o^{(1)}$, $\mathbf{x}_o^{(2)}$, and $\mathbf{x}_o^{(3)}$. We would like to know the relationship of the three phases. For this purpose, we construct a Bayesian Network (BN) relating these variables, modeling the probability of networks beginning with a particular phase $\mathbf{x}_{o}^{(1)}$, the probability that $\mathbf{x}_{o}^{(2)}$ follows $\mathbf{x}_{o}^{(1)}$, and the probability that $\mathbf{x}_o^{(3)}$ follows $\mathbf{x}_o^{(2)}$. In other words, we estimate the distributions $p\left(\mathbf{x}_o^{(1)}\right), p\left(\mathbf{x}_o^{(2)}|\mathbf{x}_o^{(1)}\right)$, and $p\left(\mathbf{x}_o^{(3)}|\mathbf{x}_o^{(2)}\right)$ by using the population history, and update these estimates during the exploitation process. New offspring solutions are created by sampling from this BN.

3 Experiments

In this section, we briefly explain the experimental setup and implementation details of NSGA-Net, followed by the empirical results to demonstrate the efficacy of NSGA-Net to automate the NAS process on image classification task in

Table 1.

Dataset. We consider the CIFAR-10 [Krizhevsky *et al.*, 2009] dataset for our classification task. We split the original training set (80%-20%) to create our training and validation sets for architecture search. The original CIFAR-10 testing set is only utilized at the conclusion of the search to obtain the test accuracy for the models on the final trade-off front.

Hyper-parameters. We set the number of phases n_p to three and the number of nodes in each phase n_o to six. The initial population is generated by uniform random sampling. The probabilities of crossover and mutation operations are set at 0.9 and 0.02 respectively. The population size is 40 and the number of generations is 20 for the exploration stage. And another ten generations for exploitation. Hence, a total of 1,200 network architectures are searched by NSGA-Net. During architecture search, we limit the number of filters (channels) in any node to 16 for each one of the generated network architecture. We then train them on our training set using stochastic gradient descent (SGD) with initial learning rate is 0.025 anneals down to zero in 25 epochs.

4 Conclusions

This paper presented NSGA-Net, a multi-objective evolutionary approach for neural architecture search. NSGA-Net affords a number of practical benefits: (1) the design of neural network architectures that can effectively optimize and trade-off multiple competing objectives, (2) advantages afforded by population-based methods being more effective than optimizing weighted linear combination of objectives, and (3) more efficient exploration and exploitation of the search space through a customized crossover scheme and leveraging the entire search history through BOA. Experimentally, by optimizing both prediction performance and computational complexity NSGA-Net finds networks that are significantly better than hand-crafted networks on both objectives and is compares favorably to other state-of-the-art single objective NAS methods for classification on CIFAR-10.

References

- [Deb et al., 2002] Kalyanmoy Deb, Amrit Pratap, Sameer Agarwal, and TAMT Meyarivan. A fast and elitist multiobjective genetic algorithm: Nsga-ii. *IEEE Transactions on Evolutionary Computation*, 6(2):182–197, 2002.
- [He *et al.*, 2016] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *CVPR*, 2016.
- [Holland, 1975] J. H. Holland. Adaptation in Natural and Artificial Systems. Ann Arbor, MI: MIT Press, 1975.
- [Huang *et al.*, 2017] Gao Huang, Zhuang Liu, Laurens Van Der Maaten, and Kilian Q Weinberger. Densely connected convolutional networks. In *CVPR*, 2017.
- [Ioffe and Szegedy, 2015] Sergey Ioffe and Christian Szegedy. Batch normalization: Accelerating deep network training by reducing internal covariate shift. 2015.
- [Juefei-Xu et al., 2017] Felix Juefei-Xu, Vishnu Naresh Boddeti, and Marios Savvides. Local binary convolutional neural networks. In CVPR, 2017.
- [Krizhevsky et al., 2009] Alex Krizhevsky, Geoffrey Hinton, et al. Learning multiple layers of features from tiny images. Technical report, Citeseer, 2009.
- [Liu et al., 2019] Hanxiao Liu, Karen Simonyan, and Yiming Yang. DARTS: Differentiable architecture search. In ICLR, 2019.
- [Lu et al., 2019] Zhichao Lu, Ian Whalen, Vishnu Boddeti, Yashesh Dhebar, Kalyanmoy Deb, Erik Goodman, and Wolfgang Banzhaf. Nsga-net: Neural architecture search using multi-objective genetic algorithm. In GECCO, 2019.
- [Pedersen and Yang, 2006] Gerulf KM Pedersen and Zhenyu Yang. Multi-objective pid-controller tuning for a magnetic levitation system using nsga-ii. In *GECCO*, pages 1737–1744. ACM, 2006.
- [Pelikan *et al.*, 1999] Martin Pelikan, David E Goldberg, and Erick Cantú-Paz. Boa: The bayesian optimization algorithm. In *GECCO*, 1999.
- [Pham *et al.*, 2018] Hieu Pham, Melody Guan, Barret Zoph, Quoc Le, and Jeff Dean. Efficient neural architecture search via parameters sharing. In *ICML*, 2018.
- [Real et al., 2017] Esteban Real, Sherry Moore, Andrew Selle, Saurabh Saxena, Yutaka Leon Suematsu, Jie Tan, Quoc V. Le, and Alexey Kurakin. Large-scale evolution of image classifiers. In *ICML*, 2017.
- [Real *et al.*, 2019] Esteban Real, Alok Aggarwal, Yanping Huang, and Quoc V Le. Regularized evolution for image classifier architecture search. In *AAAI*, 2019.
- [Sandler *et al.*, 2018] Mark Sandler, Andrew Howard, Menglong Zhu, Andrey Zhmoginov, and Liang-Chieh Chen. Mobilenetv2: Inverted residuals and linear bottlenecks. In *CVPR*, 2018.
- [Simonyan and Zisserman, 2015] Karen Simonyan and Andrew Zisserman. Very Deep Convolutional Networks for Large-scale Image Recognition. In *ICLR*, 2015.

- [Szegedy *et al.*, 2015] Christian Szegedy, Wei Liu, Yangqing Jia, Pierre Sermanet, Scott Reed, Dragomir Anguelov, Dumitru Erhan, Vincent Vanhoucke, and Andrew Rabinovich. Going deeper with convolutions. In *CVPR*, 2015.
- [Tapia and Coello, 2007] Ma Guadalupe Castillo Tapia and Carlos A Coello Coello. Applications of multi-objective evolutionary algorithms in economics and finance: A survey. In *CEC*, pages 532–539. IEEE, 2007.
- [Xie and Yuille, 2017] L. Xie and A. Yuille. Genetic CNN. In ICCV, 2017.
- [Zagoruyko and Komodakis, 2016] Sergey Zagoruyko and Nikos Komodakis. Wide residual networks. In BMVC, 2016
- [Zhang et al., 2018] Xiangyu Zhang, Xinyu Zhou, Mengxiao Lin, and Jian Sun. Shufflenet: An extremely efficient convolutional neural network for mobile devices. In CVPR, 2018.
- [Zoph and Le, 2016] B. Zoph and Q. V. Le. Neural Architecture Search with Reinforcement Learning. *arXiv preprint arXiv:1611.01578*, 2016.
- [Zoph *et al.*, 2018] Barret Zoph, Vijay Vasudevan, Jonathon Shlens, and Quoc V Le. Learning transferable architectures for scalable image recognition. In *CVPR*, 2018.